

58 The time to maximum height is 2.5s. Calculate  $v_0$  using kinematics

$$v_0 = ? \quad v_f = 0 \quad t = 2.5s \quad a = -9.8 \text{ m/s}^2 \quad X_i = 0 \quad X_f = ?$$

$$v_f = v_0 + at \Rightarrow v_0 = v_f - at = 0 - (-9.8)(2.5)$$
$$v_0 = 24.5 \text{ m/s}$$

Now find  $X_f$  at  $t = 1.5s$ .

$$X_f = X_i + v_0 t + \frac{1}{2} at^2$$
$$= 0 + 24.5 \times 1.5 + \frac{1}{2} (-9.8)(1.5)^2$$
$$= 36.75 - 11.025$$
$$= \boxed{25.7 \text{ m}}$$

71 Equation of motion for the car

$$v_{0c} = 0 \quad v_{fc} = ? \quad X_{fc} = ? \quad X_{ic} = 0 \quad a_c = 2.2 \text{ m/s}^2 \quad t = t$$

$$X_{fc} = X_{ic} + v_0 t + \frac{1}{2} at^2$$
$$X_{fc} = 0 + 0 + \frac{1}{2} 2.2 t^2$$

$$X_{fc} = 1.1 t^2$$

Equation of motion for the truck  $\boxed{a=0}$

$$X_{ft} = v_c t = 9.5 t$$

The car will pass the truck when  $X_{fc} = X_{ft}$

$$1.1 t^2 = 9.5 t$$

$$t = 8.64 \text{ s}$$

The position of the car at this time is

$$(a.) \quad X_c = 1.1 \times 8.64^2 = 82 \text{ m from light}$$

71(cont) (b) At  $t = 8.64\text{s}$  the speed of the car is

$$v_{fc} = v_0 + at = 0 + 2.2 \times 8.64 = \boxed{19\text{ m/s}}$$

74! The trip is in 2 parts - the first part has  $a = g$  the second part in the water has  $a = 0$ .

Part 1. Set axes with  $+x$  downward ie  $g = +9.8\text{ m/s}^2$

$$x_0 = 0 \quad x_f = 5.2\text{ m} \quad v_0 = 0 \quad v_f = ? \quad a = 9.8\text{ m/s}^2 \quad t = ?$$

- Find  $v_f$  and  $t$ .

$$x_f = x_0 + v_0 t + \frac{1}{2} at^2$$

$$t = \sqrt{\frac{2x_f}{a}} = \sqrt{\frac{2 \times 5.2}{9.8}} = 1.03\text{ s}$$

$$v_f = v_0 + at = 0 + 9.8 \times 1.03 = 10\text{ m/s}$$

- Now for the second part of the trip  $a = 0$  and  $v = 10\text{ m/s}$ . The time for the second part is  $4.80 - 1.03 = 3.77\text{ s}$ .

$$x_f - x_0 = vt = 10 \times 3.77 = 37.7\text{ m}$$

(a) The lake is  $37.7\text{ m}$  deep.

(b) Average velocity  $v_{\text{ave}} = \frac{x_f - x_i}{t} = \frac{(37.7 + 5.2) - 0}{4.8} = +8.94\text{ m/s}$ .

$+$  in this case means downwards as I chose the  $x$  direction to be down initially.

If the lake was empty then we have a constant acceleration kinematics problem with the following conditions

$$x_i = 0 \quad x_f = 42.9 \quad v_i = ? \quad v_f = ? \quad a = +9.8 \text{ m/s}^2 \quad t = 4.8$$

(note +x is still downwards ie  $a = +9.8 \text{ m/s}^2$ )

$$x_f = x_i + v_i t + \frac{1}{2} a t^2$$

$$\left( \frac{x_f - x_i - \frac{1}{2} a t^2}{t} \right) = v_i$$

$$\left( \frac{42.9 - 0 - \frac{1}{2} 9.8 \times 4.8^2}{4.8} \right) = v_i$$

$$v_i = -14.6 \text{ m/s}$$

ie the lead ball is thrown upwards with an initial velocity of  $14.6 \text{ m/s}$ .

$$86) \quad v_r = 72 \text{ km/hr} = 72 \frac{\text{km}}{\text{hr}} \times \frac{1000 \text{ m}}{\text{km}} \times \frac{1 \text{ hr}}{3600 \text{ s}} = 20 \text{ m/s}$$

$$v_g = 144 \text{ km/hr} = 144 \frac{\text{km}}{\text{hr}} \times \frac{1000 \text{ m}}{\text{km}} \times \frac{1 \text{ hr}}{3600 \text{ s}} = 40 \text{ m/s}$$

Stopping distance of green train

$$x_f = x_i + v_i t + \frac{1}{2} a t^2 \quad v_f^2 = v_i^2 + 2a(x_f - x_i)$$

$$v_f = 0 \quad v_i = 40 \text{ m/s} \quad a = -1 \text{ m/s}^2$$

$$x_f - x_i = \frac{v_f^2 - v_i^2}{2a} = \frac{0 - 40^2}{-2} = 800 \text{ m}$$

For the red train by same manner  $x_f - x_i = 200 \text{ m}$

ie The combined distance is  $1000 \text{ m}$  so they collide.

The slower red train stops after  $20 \text{ s}$  at a distance of  $200 \text{ m}$ . So  $v_r = 0$  at collision.

The green train is still moving when it reaches the 200 m point. The kinematic equation for the position of the green train  $X_g$  is given by

$$X_g = 950 - 40t + 0.5t^2$$

At what time does the collision occur? When

$$X_g = 200$$

$$200 = 950 - 40t + 0.5t^2$$

$$\text{or } t^2 - 80t + 1500 = 0$$

$$(t - 30)(t - 50) = 0$$

ie when  $t = 30\text{s}$ .

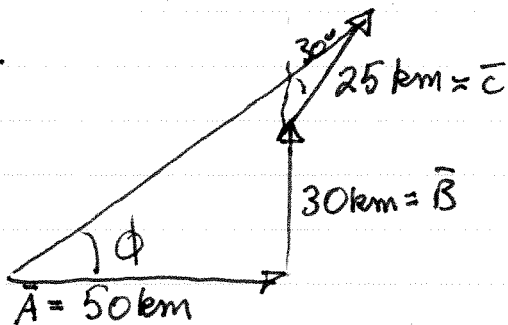
What is the speed of the green train at  $t = 30\text{s}$

$$v_g = -40 + t$$

ie  $v_g = -10\text{ m/s}$  ie moving in the negative x at 10 m/s.

### Chapter 3

8.



$$\vec{R} = \vec{A} + \vec{B} + \vec{C}$$

$$R_x = 50 + 0 + 25 \sin 30$$

$$= 62.5$$

$$R_y = 0 + 30 + 25 \cos 30$$

$$= 51.7$$

$$|R| = \sqrt{62.5^2 + 51.7^2} = 81 \text{ km}$$

$$\tan \phi = \frac{51.7}{62.5} \Rightarrow \phi = 40^\circ$$

### 9. Add components

$$\vec{c} = \vec{a} + \vec{b}$$

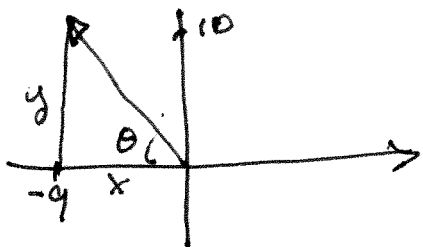
$$c_x = a_x + b_x = 4 - 13 = -9$$

$$c_y = a_y + b_y = 3 + 7 = +10$$

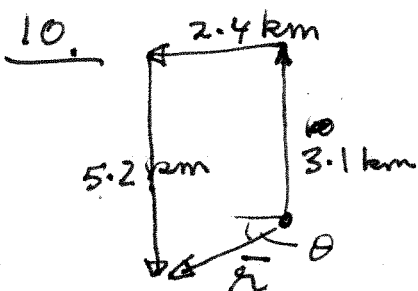
$$\vec{c} = -9\hat{i} + 10\hat{j}$$

$$|\vec{c}| = \sqrt{9^2 + 10^2} = \sqrt{181} = 13.5$$

$$\tan \theta = \left| \frac{10}{-9} \right| = 48^\circ \quad \leftarrow \text{to figure out the meaning of the angle draw } \vec{c}.$$



If they asked for the angle with respect to +x it would be  $138^\circ$ .



$$\vec{a} = 3.1\hat{j} \quad \vec{b} = -2.4\hat{i} \quad \vec{c} = -5.2\hat{j}$$

$$\vec{r} = \vec{a} + \vec{b} + \vec{c}$$

$$= -2.4\hat{i} + (3.1 - 5.2)\hat{j}$$

$$= -2.4\hat{i} - 2.1\hat{j}$$

$$|\vec{r}| = \sqrt{2.4^2 + 2.1^2} = 3.2 \text{ km}$$

$$\tan \theta = \left| \frac{r_y}{r_x} \right| = \left| \frac{2.1}{2.4} \right| \Rightarrow \theta = 41.2$$

### 13. (a) Add components

$$\vec{a} + \vec{b} = (a_x + b_x)\hat{i} + (a_y + b_y)\hat{j} + (a_z + b_z)\hat{k}$$

$$= (4 - 1)\hat{i} + (-3 + 1)\hat{j} + (1 + 4)\hat{k}$$

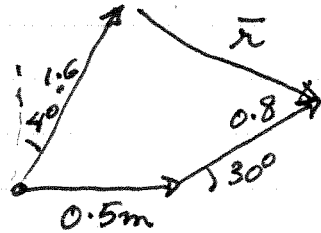
$$= 3\hat{i} - 2\hat{j} + 5\hat{k}$$

(b)  $\vec{a} - \vec{b} = 5\hat{i} - 4\hat{j} - 3\hat{k}$

13 (c)  $\vec{a} - \vec{b} + \vec{c} = 0 \Rightarrow \vec{c}$ 's components must zero out each component of  $(\vec{a} - \vec{b})$

$$\Rightarrow \vec{c} = -5\hat{i} + 4\hat{j} + 3\hat{k}$$

24



Find  $\vec{r}$ .

$$\vec{b}_1 = (0.5 + 0.8 \cos 30)\hat{i} + 0.8 \sin 30\hat{j}$$

$$\vec{b}_2 = 1.6 \sin 40\hat{i} + 1.6 \cos 40\hat{j}$$

$$\vec{r} = \vec{b}_1 - \vec{b}_2 = (0.5 + 0.8 \cos 30 - 1.6 \sin 40)\hat{i} + (0.8 \sin 30 - 1.6 \cos 40)\hat{j}$$

$$\vec{r} = -0.03\hat{i} - 0.83\hat{j}$$

almost zero.

$$\Rightarrow |\vec{r}| = 0.83\text{m south.}$$